Write your name here
 Mathematics B
Paper 1

Wednesday 14 May 2014 - Morning Time: 1 hour 30 minutes

You must have: Ruler graduated in centimetres and millimetres,
Total Marks protractor, compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided - there may be more space than you need.
- Calculators may be used.


## Information

- The total mark for this paper is 100.
- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.
- Without sufficient working, correct answers may be awarded no marks.



## Answer ALL TWENTY-EIGHT questions.

Write your answers in the spaces provided.
You must write down all stages in your working.

1 Simplify $\frac{4 x+12}{x^{2}+3 x}$

2


Diagram NOT
accurately drawn

The volume of a right circular cylinder of height 13 cm is $117 \pi \mathrm{~cm}^{3}$.
Calculate, in cm , the radius of the cylinder.

3 Express 625 grams as a fraction of 1 kilogram. Give your answer in its simplest form.

4 Calculate the size, in degrees, of an exterior angle of a 24 -sided regular polygon.

5 Solve $\frac{2 x}{x+3}=1$

$$
x=
$$

6 Evaluate $\frac{7.2 \times 10^{-3}-8.4 \times 10^{-4}}{3.6 \times 10^{-1}}$, giving your answer to
(a) 3 significant figures,
(b) 3 decimal places.

7 The bearing of $A$ from $B$ is $048^{\circ}$
Calculate the bearing of $B$ from $A$.

8 Simplify $\left(\frac{a^{6}}{8}\right)^{\frac{2}{3}}$

9 The $n$th term of a sequence is $2 n-1$
Find the difference between the $(n+1)$ th term and the $n$th term of this sequence.

10 Find the Highest Common Factor (HCF) of 30, 36 and 138
Show your working clearly.

11 Make $a$ the subject of $(x-a)(x+b)=3 b x$
Write your answer as a single algebraic fraction.

$$
a=
$$

$\qquad$

12


Diagram NOT accurately drawn

In the diagram, $A B C D$ is a circle with centre $O$ and diameter $A D$.
Given that $\angle A B C=110^{\circ}$, calculate the size, in degrees, of $\angle C O D$.
Give reasons for your working.

13 Express $\sqrt{245}-\sqrt{45}$ in the form $4 \sqrt{m}$ where $m$ is a prime number.
Show all your working.

14 A cycle is travelling along a horizontal road. The diameter of each wheel of the cycle is 59 cm and each wheel makes 110 revolutions a minute.

Calculate the distance, in km to 3 significant figures, travelled by the cycle in one hour.

15


Diagram NOT
accurately drawn

The diagram shows an inverted hollow right circular cone of height $h \mathrm{~cm}$.
The area of the open end of the cone is $280 \mathrm{~cm}^{2}$. Water is poured into the cone to a height of 9 cm . The area of the surface of the water is $70 \mathrm{~cm}^{2}$, as shown in the diagram.

Calculate the value of $h$.
$16 y$ varies directly as the cube of $x$.
$y=9$ when $x=2$
Find the value of $x$ when $y=72$

17 Solve the simultaneous equations

$$
\begin{gathered}
2 x-y=2 \\
x+3 y=15
\end{gathered}
$$

18 The time at which the first goal was scored in a number of football matches was recorded.

The incomplete table and histogram give information about the time interval in which the first goal was scored and the number of matches in which the first goal was scored in that interval.

| Time $(\boldsymbol{t})$ in minutes | Number of matches |
| :---: | :---: |
| $0<t \leqslant 40$ | 20 |
| $40<t \leqslant 45$ | 35 |
| $45<t \leqslant 55$ | 50 |
| $55<t \leqslant 75$ |  |
| $75<t \leqslant 90$ |  |


(a) Use the histogram to complete the table.
(b) Use the table to complete the histogram.

19 A mixture of sand and cement is to be used to plaster a wall.
In the original mixture, the ratio of sand to cement by weight is $3: 1$
Given that the weight of sand used is 9 kg ,
(a) write down the weight, in kg , of cement used in the original mixture.
$\qquad$

It is decided to use the same weight of cement but to change the ratio of sand to cement by weight to $5: 1$ for a new mixture.
(b) Calculate the weight of sand, in kg , that has to be added to the original mixture to make the new mixture.

20 Solve the equation

$$
4 x^{2}-3 x-2=0
$$

Give your solutions to 3 significant figures.

21 Some workers were asked how they travel to work.
Of these workers
38 travel to work by bus ( $B$ ),
27 travel to work by train ( $T$ ),
5 do not travel to work by bus or by train,
$x$ travel to work by both bus and train.
(a) Using this information, complete the Venn diagram, giving your answers in terms of $x$ where appropriate.


Given that the number of workers asked is 50,
(b) calculate the value of $x$.

$$
x=.
$$

One of the workers is chosen at random.
(c) Find the probability that this worker travels to work only by bus.

22 The coordinates of $A$ are $(1,1)$ and the coordinates of $B$ are $(2,3)$.
(a) Write down the vector $\overrightarrow{A B}$ in the form $\binom{m}{n}$, where $m$ and $n$ are integers.
(b) Given that $2 \overrightarrow{A B}=\overrightarrow{A C}$, find the coordinates of $C$.

(2)
(c) Calculate the modulus, to 3 significant figures, of $\overrightarrow{A C}$.


The diagram shows a right-angled triangle $A B C$, with $B C=11 \mathrm{~cm}$ and $\angle A B C=15^{\circ}$
(a) Calculate the length, in cm to 3 significant figures, of $A B$.
$\qquad$

The point $D$ on $A B$ is such that $A D=A C$.
(b) Calculate the length, in cm to 3 significant figures, of $D B$.


The diagram shows $\triangle A B C$.
Leaving in all your construction lines, construct
(a) the perpendicular bisector of $B C$,
(b) the bisector of $\angle A B C$.

The region $\mathbf{R}$ within $\triangle A B C$ is the set of points that are closer to $B C$ than to $A B$ and are closer to $B$ than to $C$.
(c) Show, by shading, the region $\mathbf{R}$. Label the region $\mathbf{R}$.

25 A shop sells potatoes in small bags and in large bags.
The weight of the potatoes in a small bag is 2.5 kg and the cost of a small bag is $£ 1.00$
(a) Calculate the cost, in $£$, of 1 kg of the potatoes in a small bag.

## £

The weight of the potatoes in a large bag is $20 \%$ more than the weight of the potatoes in a small bag. The cost of a large bag is $11 \%$ more than the cost of a small bag.
(b) Calculate the cost, in $£$, of 1 kg of the potatoes in a large bag.
$£$.

26 (a) Show that $(x+3)$ is a factor of $2 x^{3}+13 x^{2}+27 x+18$
(b) Hence factorise completely $2 x^{3}+13 x^{2}+27 x+18$

27 An archer shoots an arrow at a target.
The probability that he will hit the target is $\frac{3}{4}$
After the first shot, the target is moved further away from the archer.
The archer shoots a second arrow at the target and the probability that he will hit the target is now $\frac{3}{5}$
(a) Complete the probability tree diagram.


Calculate the probability that the archer will
(b) hit the target with his first shot but miss the target with his second shot,
(c) hit the target at least once if he takes both shots.

28


The diagram shows a rectangle $A C E G$ of length 20 cm and width 10 cm .
The rectangle $B C D S$ and the square $H S F G$ are shown shaded.
The square $H S F G$ has sides of length $x \mathrm{~cm}$.
The total area of the rectangle $B C D S$ and the square $H S F G$ is $y \mathrm{~cm}^{2}$.
(a) Show that $y=2 x^{2}-30 x+200$
(b) Find the value of $x$ for which $y$ is a minimum.
$\qquad$
(c) Hence find the minimum total area, in $\mathrm{cm}^{2}$, of the rectangle $B C D S$ and the square $H S F G$.
$\mathrm{cm}^{2}$

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