Please check the examination details below before entering your candidate information


## Monday 7 January 2019



You must have: Ruler graduated in centimetres and millimetres, Total Marks protractor, compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided - there may be more space than you need.
- Calculators may be used.


## Information

- The total mark for this paper is 100 .
- The marks for each question are shown in brackets - use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.
- Without sufficient working, correct answers may be awarded no marks.


## Answer ALL TWENTY EIGHT questions.

Write your answers in the spaces provided.

## You must write down all the stages in your working.

1 Express 15 centimetres as a percentage of 3 metres.

2

A

B

The diagram shows shape $\mathbf{A}$ and shape $\mathbf{B}$.
Write down,
(a) the number of lines of symmetry of shape $\mathbf{A}$,
(b) the order of rotational symmetry of shape $\mathbf{B}$.

3 The bearing of ship $P$ from ship $Q$ is $057^{\circ}$
Find the bearing of ship $Q$ from ship $P$.

Calculate $3 \mathbf{A}+2 \mathbf{B}$

5 Without using a calculator and showing all your working, evaluate

$$
2 \frac{1}{4} \times 2 \frac{2}{3}
$$

Give your answer in its simplest form.

6 Given that $y=7 x^{2}-\frac{3}{x}$
find $\frac{\mathrm{d} y}{\mathrm{~d} x}$

$$
\frac{\mathrm{d} y}{\mathrm{~d} x}=
$$

7 Here are the first 4 terms of a sequence.
$4096 \quad-1024 \quad 256 \quad-64$
(i) Write down the next 2 terms of the sequence.
(ii) Explain how you found your answer.

8 Ying has 4 black counters and 3 white counters.
There is a number on each counter.
The mean of the numbers on the black counters is 11.5
The mean of the numbers on the white counters is 9
Calculate the mean, to 3 significant figures, of the numbers on all 7 counters.

9 Find the largest integer value of $x$ such that $17-2 x \geqslant 4(x-5)$
Show clear algebraic working.

10 A regular polygon has $n$ sides.
Each interior angle of the regular polygon is $135^{\circ}$ greater than each exterior angle of the polygon.

Find the value of $n$.

$$
n=
$$

(Total for Question 10 is 3 marks)

11 A piece of ribbon 9 metres long is cut into 3 parts in the ratios $3: 5: 7$ by length.
Calculate the length, in metres, of the longest piece.

12 (a) Write $9.6 \times 10^{-7}$ as an ordinary number.
(b) Calculate $\frac{2.4 \times 10^{199}}{9.6 \times 10^{-7}}$

Give your answer in standard form.
(2)

13 Without using a calculator and showing all your working, express

$$
\sqrt{605}-\sqrt{80}
$$

in the form $\sqrt{n}$ where $n$ is an integer.

14 Solve the equation

$$
5 x^{2}=7-9 x
$$

Give your solutions to 3 significant figures.
Show your working clearly.

15


The diagram shows quadrilateral $A B C D$.
The point $P$ lies inside the quadrilateral, such that $P$ is 5.5 cm from $C$ and equidistant from $A D$ and $A B$.

Using ruler and compasses only and showing all your construction lines, show the point $P$ on the diagram.
(Total for Question 15 is 4 marks)
$16 t$ varies inversely as the square of $a$ where $a>0$ $t=14$ when $a=5$

Calculate the value of $a$ when $t=224$

A

B

The diagram shows two similar jugs.
The height of jug $\mathbf{A}$ is 20 cm and the height of jug $\mathbf{B}$ is 6 cm .
Given that
volume of jug $\mathbf{A}-$ volume of jug $\mathbf{B}=1459.5 \mathrm{~cm}^{3}$
calculate the volume, in $\mathrm{cm}^{3}$, of jug $\mathbf{B}$.
$18 \mathscr{E}=$ \{positive integers from 1 to 15 inclusive $\}$
$A=\{$ multiples of 3$\}$
$B=\{$ even numbers $\}$
(a) Find $A \cup B$

$$
\begin{equation*}
A \cup B=\{ \tag{1}
\end{equation*}
$$

(b) (i) Find $A \cap B$

$$
\begin{equation*}
A \cap B=\{ \tag{1}
\end{equation*}
$$

(ii) Find $\mathrm{n}\left([A \cap B]^{\prime}\right)$

$$
\begin{equation*}
\mathrm{n}\left([A \cap B]^{\prime}\right)= \tag{1}
\end{equation*}
$$

The set $C$ has 8 elements and $B \cap C=\varnothing$
(c) Write down the elements of $\operatorname{set} C$.

$$
C=\{
$$

19 Solve the simultaneous equations

$$
\begin{aligned}
& 10 x+2 y=17 \\
& 15 x-3 y=39
\end{aligned}
$$

20 The coordinates of point $A$ are $(7,2)$ and the coordinates of point $B$ are $(-5, y)$.
The modulus of the vector $\overrightarrow{A B}$ is 13
Calculate the possible values of $y$.

$$
y=
$$

21 The straight line joining the points with coordinates $(-a,-22)$ and $(3 a, 38)$ has equation $y=m x+a$

Calculate the value of $a$ and the value of $m$.
$a=$
$m=$

22


Diagram NOT accurately drawn

In the diagram $A C E$ and $B C D$ are straight lines such that the point $C$ is the midpoint of $B D$.
$A B$ is parallel to $D E$.
Prove that the triangles $A B C$ and $E D C$ are congruent.

23 A right circular cone has a curved surface area of $136 \pi \mathrm{~cm}^{2}$ The radius of the base of the cone is 8 cm The volume of the cone is $k \pi \mathrm{~cm}^{3}$

Find the value of $k$.

24 Solve $3-\frac{x+1}{2 x^{2}+9 x-5}-\frac{2 x-1}{x+5}=1$
Show clear algebraic working.

$$
x=
$$

25 There are 20 counters in a bag.
There are 7 red counters.
The rest of the counters are green or white.
Bernard takes at random 2 counters from the bag.
The probability that Bernard will take 2 white counters is $\frac{1}{19}$
Calculate the probability that Bernard will take 1 green counter and 1 white counter.

26 The table below gives information about the lengths of time that 50 people have been waiting for a train.

| Waiting time ( $\boldsymbol{m}$ minutes) | Frequency |
| :---: | :---: |
| $0<m \leqslant 5$ | 4 |
| $5<m \leqslant 10$ | 5 |
| $10<m \leqslant 15$ | 11 |
| $15<m \leqslant 20$ | 8 |
| $20<m \leqslant 25$ | 22 |

(a) Find the modal class.
(b) Find the class interval that contains the median waiting time.
(c) Calculate an estimate for the mean waiting time.

## minutes

(3)


Diagram NOT accurately drawn

The diagram shows $\triangle A B C$ in which

$$
A B=(2 x-5) \mathrm{cm} \quad B C=(x+5) \mathrm{cm} \quad \angle A B C=30^{\circ}
$$

The area of $\triangle A B C$ is $15.75 \mathrm{~cm}^{2}$
Calculate the length, in cm to 3 significant figures, of $A C$.

28 (a) Factorise fully $15 x^{3} y-20 x^{2} y^{2}$
(2)
(b) Simplify fully $\frac{\left(27 x^{6}\right)^{\frac{2}{3}}}{18 x^{3}}$
(c) Given that $(x-2)$ is a factor of $2 x^{3}+3 x^{2}+k x-6$
find the value of $k$.
(2)

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